



## Structural modulation of graphene by an external electric field



Nadia Sultana\*, Yanlin Gao, Mina Maruyama and Susumu Okada\*

Department of Physics, University of Tsukuba, 1-1-1 Tennodai, Tsukuba 305-8571, Ibaraki, Japan

\*Corresponding author: e-mail address: [nsultana@comas-tsukuba.jp](mailto:nsultana@comas-tsukuba.jp); e-mail address: [sokada@comas-tsukuba.jp](mailto:sokada@comas-tsukuba.jp)*This is an open-access article distributed under the Creative Commons Attribution License CC BY-SA 4.0*

### ARTICLE INFO

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### ABSTRACT

The geometric structure of graphene under an external electric field was investigated using the density functional theory (DFT). DFT calculations revealed that the hole injection into graphene highly modulates the geometric structure of graphene. The lattice parameter of graphene monotonically increased with increasing the hole doping concentration. The lattice constant is insensitive to the electron doping. The fragility and robustness against the hole and electron doping, respectively, are ascribed to the electronic structure of graphene under the electric field. The wave function analysis revealed that the holes are accommodated in the bonding  $\pi$  states, weakening covalent bonds between C atoms. In contrast, the electrons are primarily accommodated in nearly free electron states with a maximum amplitude above and below the graphene layer.

### 1. Introduction

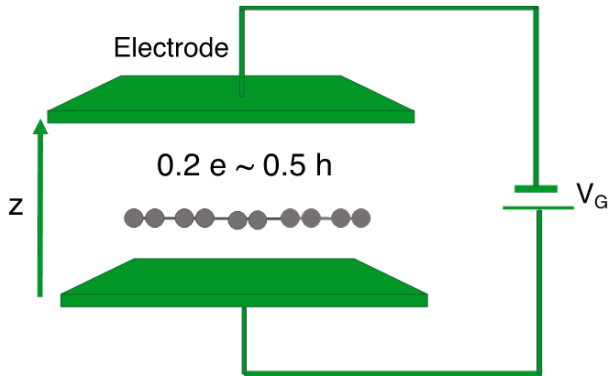
Since its discovery, graphene has attracted scientific and technological interest due to its excellent physical properties resulting from its honeycomb covalent network of C atoms with atom thickness [1,2]. The honeycomb covalent network of  $sp^2$  C atoms gives graphene high chemical stability, remarkable mechanical stiffness, and out-of-plane flexibility [3-5]. In addition to these structural properties, the itinerant electrons on the honeycomb network led to the unique electronic structure at and around the Fermi level and the K point in the hexagonal Brillouin zone [6,7]. Graphene possesses conical dispersion bands at the Fermi level that cause the remarkable carrier mobility of 200000  $cm^2/Vs$  or more [8,9]. Therefore, graphene is regarded as an emerging material for fabricating functional devices in wide fields of modern technologies. In addition to those properties of isolated graphene, graphene is considered a building block of various complexes by stacking with the other graphene layers and other atomic layer materials, such as hBN and transition-metal dichalcogenide [10,11]. These complexes show further unique physical properties that exceed the simple superposition of physical properties of constituent layers [12-13]. The conical dispersion band of graphene is fragile by forming a heterostructure with hBN [13]. More interestingly, bilayer graphene shows unique variations in their electronic structures, which are sensitive to their interlayer stacking arrangement [14,15]. An external electric field or excess

carriers on graphene and its derivatives is another essential control parameter of their physical properties. In the case of bilayer graphene with AB stacking arrangement and thin films with ABC stacking arrangement, a perpendicular electric field can create a finite band gap whose width depends on the field strength [16-19]. Furthermore, the field or excess carrier can control the Fermi energy of graphene concerning the Dirac point, increasing the current density throughout the channel of the field effect devices. These facts indicate that the electric field is decisive in determining the electronic properties of graphene and its complexes. Despite these physical insights into the field effect on electronic properties, the field effect on the structural properties of graphene is still unclear. This knowledge is crucial for practical applications of graphene because the electronic properties of graphene and its derivatives are sensitive to their geometries. Therefore, this paper aims to clarify the geometric structure of graphene with excess carriers, which are injected by the external electric field, using the density functional theory combined with the effective screening medium method.

### 2. Calculation Method

All calculations are performed in the framework of density functional theory (DFT) implemented in the Simulation Tool for Atom TEchnology (STATE) program package [20,21]. The exchange-correlation potential energy between the interacting electrons is expressed using the generalized gradient approximation with a Perdew-Burke-Ernzerhof functional [22]. Interaction between the valance electrons and

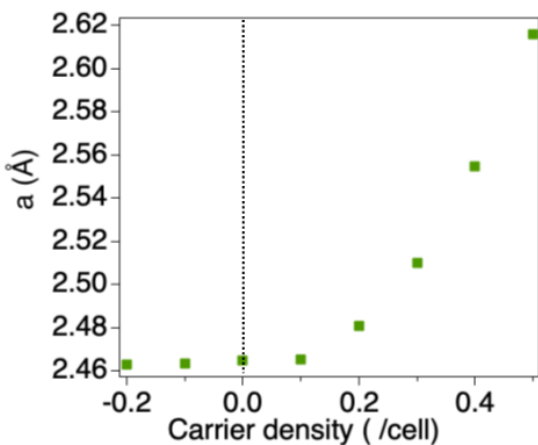
ions is treated using an ultrasoft pseudopotential generated by the Vanderbilt scheme [23]. To inject electrons or holes into graphene implemented in field effect transistors, we used the effective screening medium method, which allowed us to directly simulate the graphene field effect transistor with a dual gate electrode simulated by the effective screening medium with infinite permittivity (Fig. 1) [24]. The gate electrodes are situated above and below the graphene layer with 5 Å vacuum spacing. Here, we investigate the geometric structure of graphene under the carrier concentrations of 0.2  $e/cell \sim 0.5 h/cell$ . Integration over the Brillouin zone was carried out using an equidistance mesh of  $21 \times 21 \times 1$   $k$  points.



**Figure 1.** A structural model of a graphene field effect transistor. Gray balls indicate the C atoms, and the green plates indicate the electrodes simulated by an effective screening medium, which are connected to a gate power source  $V_G$ .

### 3. Result and discussion

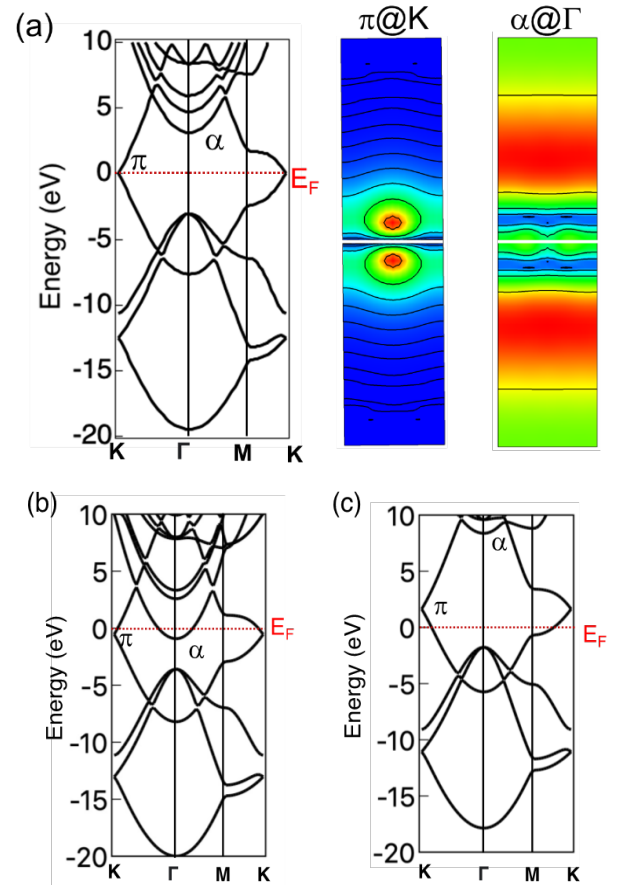
Figure 2 shows the lattice parameter of monolayer graphene under excess carriers by the external gate voltages. The lattice parameter shows a different characteristic after injecting the excess electrons and holes. The lattice parameter increases with the increase in hole density. The lattice parameter is 2.61 Å under the hole doping concentration of 0.5  $h/cell$ , which is longer by 0.15 Å than that under the neutral condition (2.46 Å). Therefore, the chemical bonds of graphene are fragile against hole injection. In contrast, the lattice parameter of graphene is robust against electron doping. The lattice parameter retains that of the neutral value under the electron concentrations of 0.1 and 0.2  $e/cell$ .



**Figure 2.** A lattice parameter of monolayer graphene as a function of carrier species and concentration. A vertical dotted line indicates the neutral position. Positive and negative values correspond to the hole and electron concentrations per unit cell, respectively.

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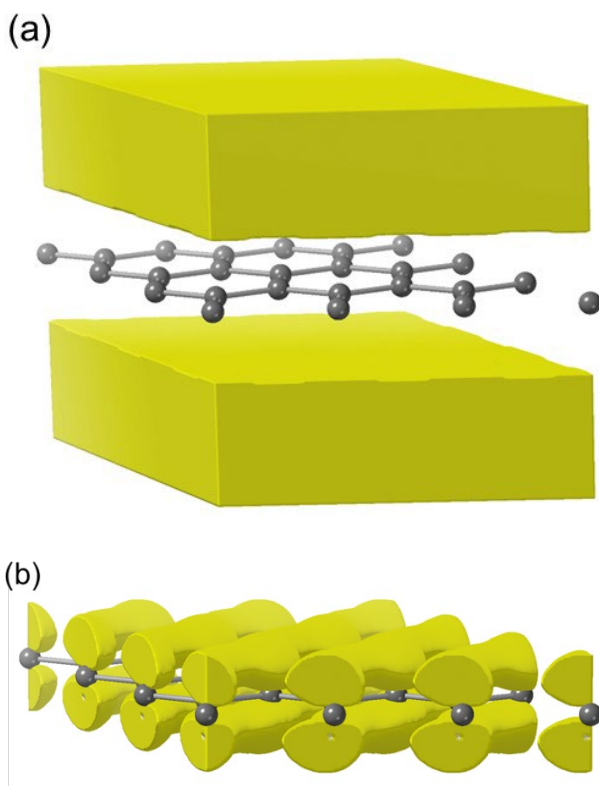


**Figure 3.** (a) Electronic structures of monolayer graphene without excess carriers. Contour plots of the squared wave functions of the Dirac point at the K point ( $\pi$ ) and the lowest branch of the conduction band at the  $\Gamma$  point with a parabolic nature (a) are depicted in the right of the panel. White horizontal lines in contour plots denote graphene layer. Electronic structures of monolayer graphene (b) under the electron concentration of 0.2  $e/cell$ , and (c) under the hole concentration of 0.2  $h/cell$  are measured from the Fermi level, which is denoted by the red dotted horizontal lines.

We investigated the electronic structure of graphene with excess carriers to provide the physical mechanism of the lattice parameter modulation of graphene. Figure 3(a) shows the electronic structures and squared wave function of the Dirac point at the K point and the lowest branch of the conduction at the  $\Gamma$  point of monolayer graphene without excess carriers. The wave function associated with the Dirac point is distributed throughout the graphene layer with  $\pi$  state nature. The wave function associated with the lowest branch of the conduction band at the  $\Gamma$  point has a unique distribution. The wave function is distributed not only on the C atomic layer but also in the vacuum spacing outside the layer known to be nearly free electron (NFE) states [7]. The carrier injection highly modulates the electronic structure of graphene. For the electron doping, the parabolic band at the  $\Gamma$  point substantially shifts downward and crosses the Fermi level, indicating the carrier injection into this NFE state. While the Dirac point at the K point is still located at the Fermi level (Fig. 3(b)). Thus, the injected electrons are primarily accommodated in the NFE states and do not affect the chemical bond of graphene. In contrast, the Fermi level substantially shifts downward under the hole injection into the graphene, clearly indicating that the

electron density of the bonding  $\pi$  states decreases by the hole injection (Fig. 3(c)). Thus, the covalent bond between C atoms is weakened, increasing the lattice parameter.

Figure 4 shows the electron and hole distribution in graphene under an electron doping concentration of  $0.2e/\text{cell}$  and hole doping concentration of  $0.2h/\text{cell}$ , respectively, by the corresponding gate voltage. The accumulated electron is not distributed on the graphene layer but in the vacuum spacing above the graphene layer. The distribution corroborated that electron doping does not affect the covalent bond of graphene. In contrast, the accumulated holes have a distribution that is the same as that of the  $\pi$  electron states of graphene. Thus, the electron density on bonding  $\pi$  states decreases by the hole doping. This electron density decrease may weaken the covalency of the honeycomb network of graphene and increase the lattice parameter with increasing the hole concentration.



**Figure 4.** Isosurfaces of accumulated (a) electron and (b) hole distributions in graphene under the electron doping concentration of  $0.2e/\text{cell}$  and hole doping concentration of  $0.2h/\text{cell}$ , respectively.

#### 4. Summary

We studied the geometric structure of graphene under the excess electrons and holes that are injected by the gate electric field in terms of the doping concentration based on density functional theory with the effective screening medium method. Our analysis revealed that the geometric structure of monolayer graphene is sensitive to hole doping, leading to the fact that the lattice parameter monotonically increases with increasing the hole concentration. In contrast, the geometric structure of graphene is insensitive to electron doping. The lattice parameter of graphene retains its value up to the electron concentration of  $0.2e/\text{cell}$ . The fragility and robustness against the carrier injection are ascribed to the electronic structure of graphene with excess carriers. The

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electron doping causes a substantial downward shift of the NFE state, which is distributed not only on the atomic layer but also in the vacuum spacing. Accordingly, the electrons are primarily accumulated in this NFE state while they do not affect the  $\pi$  electron states. Therefore, the covalent bond is insensitive to the electron concentration. In contrast, the holes are accommodated in bonding  $\pi$  states. Thus, the hole doping weakens the covalent bonds, and the lattice parameter increases with the increase of the hole concentration.

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#### **Ethical Approval:**

The submitted work is a unique contribution to the field, not published elsewhere in any form or language. Results are presented clearly, honestly, and without fabrication, falsification or inappropriate data manipulation (including image-based manipulation). Authors adhere to discipline-specific rules for acquiring, selecting and processing data.

#### **Consent of Participate:**

The submitted work is theoretical work on atomic layer materials. No human subject or living organism/tissue is involved in this research.

#### **Consent to Publish:**

No consent to publish is to be shared.

#### **Author Contributions**

All authors contributed to the study conception and design. Design and analysis were performed by Nadia Sultana. The first draft of the manuscript was written by Nadia Sultana and all authors commented on previous versions of the manuscript. All authors read and approved the final manuscript.”